

Decision Deck



## Multiple Criteria Decision Aiding in action

### Decision Deck & diviz

**Miłosz Kadziński**

milosz.kadzinski@cs.put.poznan.pl

- 1 : Institute of Computing Science, Poznan University of Technology, Poznań, Poland
- 2 : Decision Deck Consortium
- 3 : EURO Working Group on MCDA & International MCDM Society
- 4 : Participant of MCDA/M Summer School in Paris (2010)

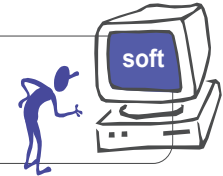
Miłosz Kadziński

Chania, July 23 – August 3, 2018

## Agenda

### How does software situation look in MCDA?

- many methods / software
- great need for unified software framework



### Decision Deck – Decision what?

- XMCDA, MCDA web services, diviz
- diviz**: design, execution and deployment tool
- live demo and "hands on training"



### A bit of methodological summary for illustrative purpose

- focus on value- and outranking based methods
- "reinvent" methods on your own



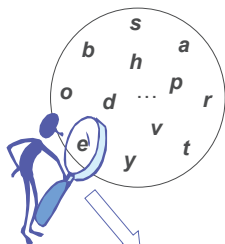
[www.cs.put.poznan.pl/mkadzinski/MCDASummerSchool/](http://www.cs.put.poznan.pl/mkadzinski/MCDASummerSchool/)

Miłosz Kadziński

Chania, July 23 – August 3, 2018

## Essence of MCDA

A = set of alternatives



INPUT

**Alternatives** are evaluated on multiple preference dimensions (**criteria**, attributes)

OUTPUT

Help to work out the **recommendation**, i.e. to determine the best alternatives, rank them or assign to ordered **classes**

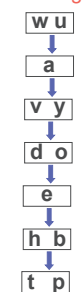
INPUT

By taking into account the **preferences** of the decision maker

sorting

w	u	a	C <sub>3</sub> =leading
v	y	d	C <sub>2</sub> =average
h	b	t	C <sub>1</sub> =weak

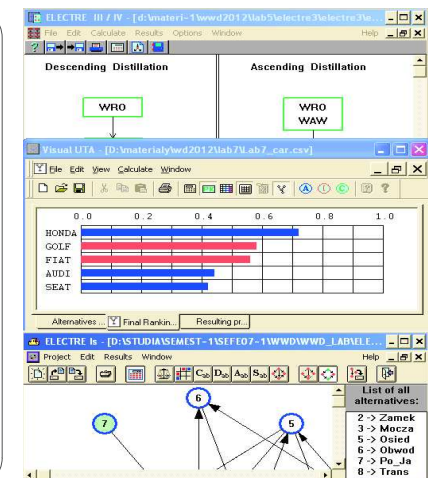
ranking



G = set of criteria

## Software situation in MCDA

- many different methods
- many **separate** software products
  - heterogeneous user interfaces
- no standard data format and unified software to test the same problem on various methods
- many algorithms **not easily available**
- often **not free** (financial and open source)
- existing MCDA methods cannot communicate



Miłosz Kadziński

Chania, July 23 – August 3, 2018

Miłosz Kadziński

Chania, July 23 – August 3, 2018

## MCDA software overview

### UTA

UTA+, Visual UTA, Right Choice, DECERNS, UTADIS

### ELECTRE

Electre Is, Electre III-IV, Electre Tri, IRIS, MCDA-ULaval

### JSMAA

VIP (MAVT)  
M-MACBETH  
jMAF (DRSA)  
1000 minds  
Quantum-GIS  
plugins  
...

### AHP/ANP

Make It Rational, Web HIPRE, Expert Choice, Decision Lens, Super Decision

### PROMETHEE

Decision Lab, D-Sight, Smart Picker Pro, Visual Promethee, DECERNS

Check software sections at the websites of EWG-MCDA and MCDM society:

- <http://www.cs.put.poznan.pl/ewgmcda/>
- <http://www.mcdmsociety.org/>

 A. Ishizaka, P. Nemery, *Multi-criteria Decision Analysis: Methods and Software*, Wiley, 2013

## Decision Deck project

### Decision Deck project

aims at collaboratively developing open source software tools implementing Multiple Criteria Decision Aiding methods and concepts



Its **purpose** is to provide effective tools to three types of users:

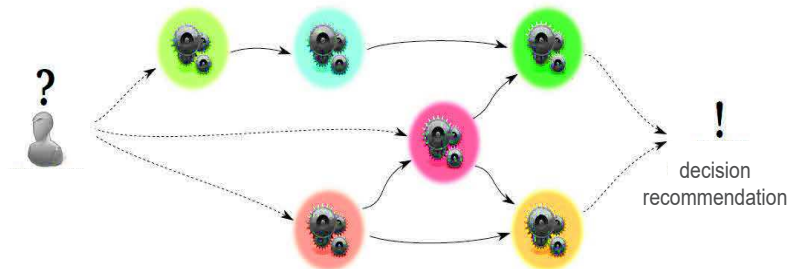
- **practitioners** (consultants / analysts) who use MCDA tools to support actual decision makers
- **researchers** who want to test, compare or develop methods
- **teachers and students** who present / use MCDA methods in courses



Promote MCDA research and make it more visible to the "outside" world

## How are MCDA methods designed?

- MCDA methods are **sequences** of *elementary* algorithms
- MCDA methods *share* a lot of **similarities**
- MCDA methods need to be **adaptable** to the given practical case



## Focus on three initiatives from Decision Deck project

### XMCD – to make algorithms interoperable

- a data standard for MCDA
- standardized format to represent objects and data structures issued from MCDA



### XMCD web services – to make algorithms easily available

- algorithmic components or complete MCDA methods accessible online
- reuse of existing implementations



### diviz – to create complex algorithmic workflows

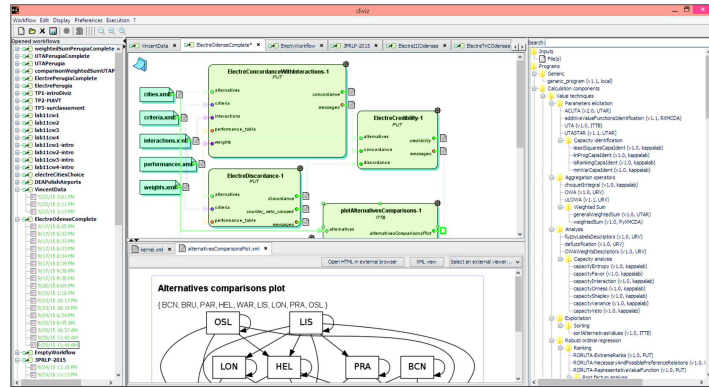
- open source Java client and server
- web services compositions, workflow management and deployment





Just download it and run - [www.diviz.org/download](http://www.diviz.org/download)

- no need to install (although possible, for different operating systems)
- platform independent jar**
- requirement for the **Internet access** and Java installed (=commonplace)



Miłosz Kadziński

Chania, July 23 – August 3, 2018

## diviz

- open source Java client and server
- a tool for designing complex MCDA workflows via the XMCD web-services



- study a *classical* multiple criteria decision problem: **Thierry's car choice problem**
- learn how to use the **diviz software**
- use diviz as a decision support tool

Miłosz Kadziński

Chania, July 23 – August 3, 2018

## The data = Thierry's choice problem

- In 1993, **Thierry**, a student aged 21, is passionate about sports cars and **wishes to buy** a middle range 4 years old car with a powerful engine
- He selects **three viewpoints** related to cost (criterion  $g_1$ ), performance of the engine (criteria  $g_2$  and  $g_3$ ) and safety (criteria  $g_4$  and  $g_5$ )
- The cost criterion  $g_1$  (€) and the performance criteria acceleration  $g_2$  (seconds) and pick up  $g_3$  (seconds) have **to be minimized**, whereas the safety criteria brakes  $g_4$  and road-hold  $g_5$  have **to be maximized**
- The values of the safety criteria are average evaluations obtained from multiple qualitative evaluations which have been re-coded as integers between 0 and 4



D. Bouyssou, T. Marchant, M. Piriot, P. Perny, A Tsoukias, P. Vincke, *Evaluation and Decision Model, A critical perspective*, Kluwer, 2000

## Thierry's choice - performance matrix

		five criteria					
fourteen alternatives	car ID	car name	cost ( $g1$ , €)	accel. ( $g2$ , s)	pick up ( $g3$ , s)	brakes ( $g4$ )	road-hold ( $g5$ )
	a01	Tipo	18342	30.7	37.2	2.33	3
	a02	Alfa	15335	30.2	41.6	2	2.5
	a03	Sunny	16973	29	34.9	2.66	2.5
	a04	Mazda	15460	30.4	35.8	1.66	1.5
	a05	Colt	15131	29.7	35.6	1.66	1.75
	a06	Corolla	13841	30.8	36.5	1.33	2
	a07	Civic	18971	28	35.6	2.33	2
	a08	Astra	18319	28.9	35.3	1.66	2
	a09	Escort	19800	29.4	34.7	2	1.75
	a10	R19	16966	30	37.7	2.33	3.25
	a11	P309-16	17537	28.3	34.8	2.33	2.75
	a12	P309	15980	29.6	35.3	2.33	2.75
	a13	Galant	17219	30.2	36.9	1.66	1.25
	a14	R21t	21334	28.9	36.7	2	2.25

Table: **Which car should Thierry buy?**

Miłosz Kadziński

Chania, July 23 – August 3, 2018

Miłosz Kadziński

Chania, July 23 – August 3, 2018

Natural **extension of the weighted sum** which takes into account the non-linearity of preferences:

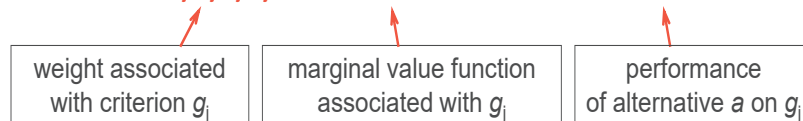
$$aPb \leftrightarrow U(a) > U(b) \quad \text{where } U(a) = f(u_1(g_1(a)), \dots, u_n(g_n(a)))$$

$$a/b \leftrightarrow U(a) = U(b)$$



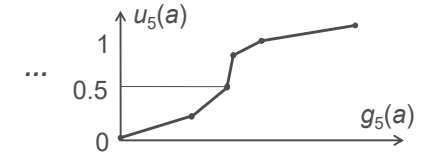
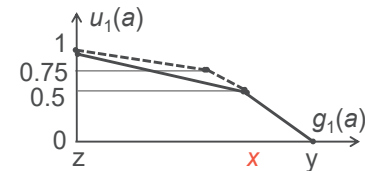
Various possible aggregation models, but here:

$$U(a) = \sum_j w_j \cdot u_j(g_j(a)) = w_1 \cdot u_1(g_1(a)) + \dots + w_n \cdot u_n(g_n(a))$$



## Step 1:

- Determine a value function  $u_j$  for each criterion such that  $u_j(g_j(a))$  represents the value of  $a$  on criterion  $g_j$ , and **read off  $u_j(g_j(a))$**  for  $g_j(a)$
- The  $u_j$  represents the decision maker's preferences (and not a normalization of the data)



For example: **bisection method**

- Define the performances that correspond to **values 0 and 1**
- Indicate a performance **x** such that changing from the 0-value performance to **x** increases the value as much as changing from **x** to the 1-value performance - the **selected midpoint** corresponds to value **0.5**
- Use the **same process** to bisect the interval of [0,0.5] and/or [0.5,1], etc.

## Step 2: determine the weights (scale coefficients) $w_j$

For example: **Rank Order Centroid (ROC) method**

- Order the criteria from **the most to the least important**

$$w_1 > w_2 > w_3 > w_4 > w_5$$

- Compute the weight for criterion with rank  $r_k$  as follows:

$$w(r_k) = 1/n \sum_{j=k \dots n} 1/j$$

$$w(r_1) = 1/5 \sum_{j=1 \dots 5} 1/j = 1/5 (1/1 + 1/2 + 1/3 + 1/4 + 1/5) = 0.457$$

$$w(r_2) = 1/5 \sum_{j=2 \dots 5} 1/j = 1/5 (1/2 + 1/3 + 1/4 + 1/5) = 0.257$$

$$w(r_3) = 0.157, w(r_4) = 0.09, w(r_5) = 0.04$$

- Weights reflect the **centroid (centre of mass) of the simplex defined by the ranking of the criteria**; they are normalized to sum up to 1

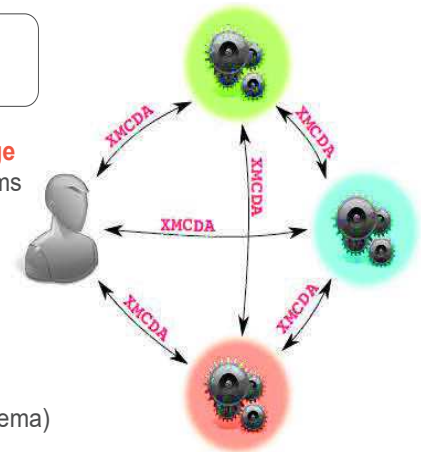
## Step 3: compute the comprehensive value of each alternative

$$U(a) = \sum_j w_j \cdot u_j(g_j(a)) = w_1 \cdot u_1(g_1(a)) + \dots + w_n \cdot u_n(g_n(a))$$

## XMCD

- a data standard for MCDA

- A unique communication **language** with and between MCDA algorithms
- **Standardization** and **unification** of multiple schools of thought
- Representation of MCDA data elements in XML according to a grammar (the XMCD XML schema)



## How to define MCDA inputs in XMCDAs?

### EXEMPLARY INPUTS

- MCDA concept = the list of alternatives

```
<alternatives>
  <alternative id="a01" name="TIPO">
    <type> real </type>
  </alternative>
  ...
  <alternative id="fictiveBest" name="IDEAL ALTERNATIVE">
    <type> fictive </type>
  </alternative>
</alternatives>
```

XMCDAs types = structures created to represent MCDA concepts

- MCDA concept = criteria weights

```
<criteriaValues mcdaConcept="Importance" name="significance">
  <criteriaValue>
    <criteriaID> g1 </criteriaID>
    <value>
      <real> 0.457 </real>
    </value>
  </criteriaValue>
  ...
</criteriaValues>
```

## How are MCDA outputs represented in XMCDAs?

### EXEMPLARY OUTPUTS

- MCDA concept = ranks of the alternatives

```
<alternativesValues mcdaConcept="alternativesRanks">
  <alternativeValue>
    <alternativeID> a01 </alternativeID>
    <value>
      <real> 3 </real>
    </value>
  </alternativeValue>
  ...
</alternativesValues>
```

XMCDAs types = structures created to represent MCDA concepts

- MCDA concept = pair-wise (preference, outranking) relations

```
<alternativesComparisons>
  <pairs>
    <pair>
      <initial> <alternativeID> a01 </alternativeID> </initial>
      <terminal> <alternativeID> a02 </alternativeID> </terminal>
    </pair>
    ...
  </pairs>
</alternativesComparisons>
```

## Quick guide to XMCDAs

- Possible to store advanced preference information on alternatives, criteria, and classes as well results typical for MCDA applications
- For details, see <http://www.decision-deck.org/xmcdas>
- In particular, have a look at the *Quick guide to XMCDAs*
- Work with **examples available on-line** (whenever anyone is using XMCDAs, (s)he is obliged to make the examples available for testing purposes)
- In order to avoid the writing of XMCDAs, **csvToXMCDAs-\* converters** are available (see practical work hereafter)

## diviz demo (1)

Help Thierry to **choose the car** which is "best" for him



**TIME FOR DEMO**  
**MAVT**

## Motivation for XMCD web services

### XMCD web-services

- MCDA algorithms which are made available for anybody over the Internet
- Reuse of existing implementations



### MCDA researchers

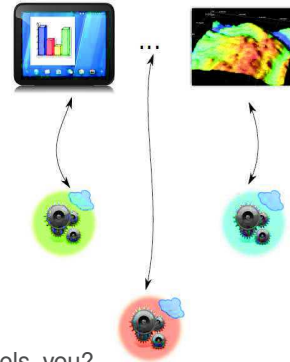
- are often not computer scientists
- have programmed their algorithms in the programming language they know best

### Idea

- allow researchers publishing their programs online
- require input / output in the XMCD format

### Maintained by the IMT Atlantique diviz team

Contributors: Poznań, Brest, Paris, Luxembourg, Tarragona, Mons, Rotterdam, Lyon, Coimbra, Brussels, you?



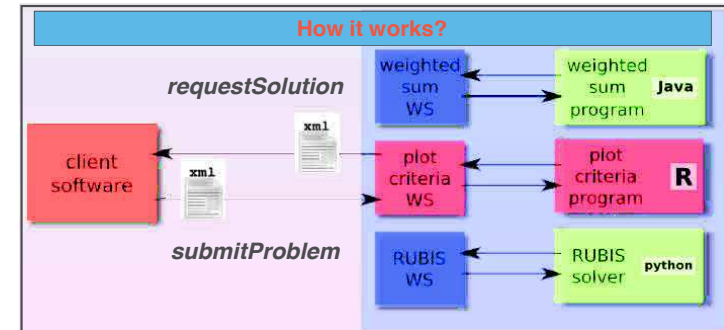
## How to use XMCD web services?

### How to use XMCD web services?

- Via various client softwares, in particular via *diviz*

### What data is exchanged?

- XML files respecting the XMCD standard



### What are the main advantages?

- Heavy calculations on a distant server in France
- Output of a web service can be reinjected into another web service

## Why XMCD web services are useful?

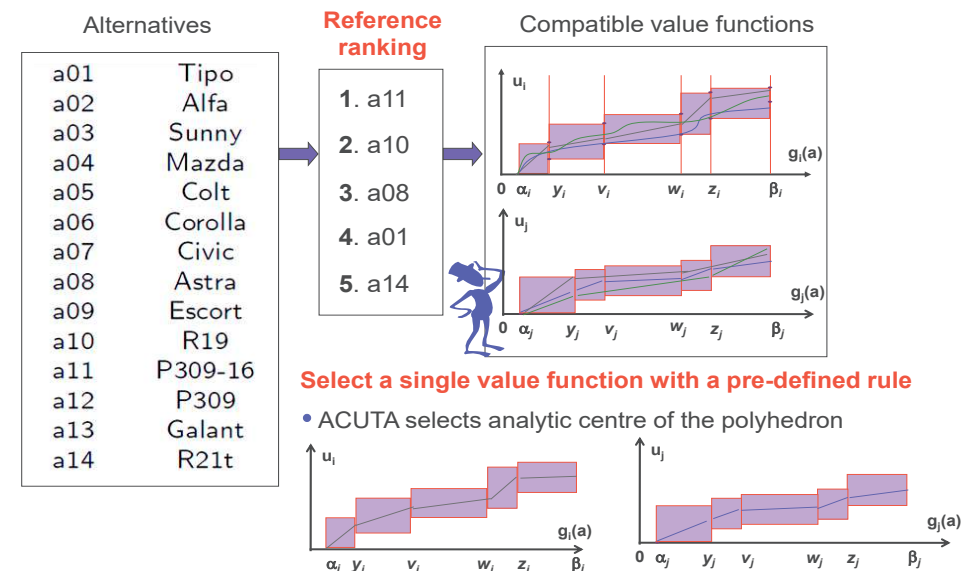
### MCDA web services

- MCDA algorithms which are made available for anybody over the Internet
- reuse of existing implementations



- Elementary procedures/algorithms available as separate software pieces
- If properly chained, they would rebuild the original method
  - Remove the black box effect of certain software
  - Better understand the heart of the methods
  - Avoid repeated implementation of the same algorithms

## UTA-like methods





## UTA-like methods: step by step

### Step 1: Provide preference information:

**ranking** (pairwise comparisons) of **reference alternatives** (e.g.,  $a_{11} > a_{10} > a_{08} > a_{01} > a_{14}$ ) and **number of segments** for each marginal value function (e.g., all marginal functions are linear = 1 linear piece)

### Step 2: Select a central value function according to a pre-defined rule

for example, **ACUTA** selects an analytic centre (UTAMP, UTASTAR, ...)

### Step 3: Compute marginal values for all alternatives

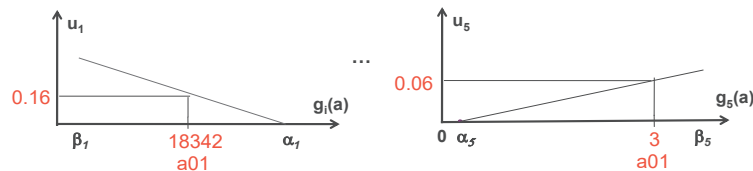
for example,  $u_1(a_{01}) = u_1(18323) = 0.16$ , etc.

### Step 4: Compute comprehensive values

for example,  $U(a_{01}) = u_1(a_{01}) + \dots + u_5(a_{01}) = 0.16 + \dots + 0.06 = 0.45$

### Step 5: Rank alternatives w.r.t. their comprehensive values

for example, 1.  $a_{03} - 0.73$ , 2.  $a_{11} - 0.71$ , ..., 12.  $a_{01} - 0.45$ , etc.



## More advanced preference information in XMCDa

### XMCDa

- modeling reference ranking
- $a_{11} > a_{10} > a_{08} > \dots$
- defining shape of marginal value functions
- one segment for  $g_1$  and  $g_2$

```
<alternativesValues>
...
<alternativeValue>
<alternativeID>a11</alternativeID>
<value>
<integer>1</integer>
</value>
</alternativeValue>
<alternativeValue>
<alternativeID>a10</alternativeID>
<value>
<integer>2</integer>
</value>
</alternativeValue>
...
</alternativesValues>
```

```
<criteriaValues
mcdaConcept="numberOfSegments">
<criteriaValue>
<criteriaID>g1</criteriaID>
<value>
<integer>1</integer>
</value>
</criteriaValue>
<criteriaValue>
<criteriaID>g2</criteriaID>
<value>
<integer>1</integer>
</value>
</criteriaValue>
...
</criteriaValues>
```

## diviz demo (2)



**TIME FOR DEMO**  
**UTA & ACUTA**

## Essence of diviz software

### diviz

- open source Java client and server
- web services compositions, workflow management and deployment



**Available components = algorithmic elements available via XMCDa web services**

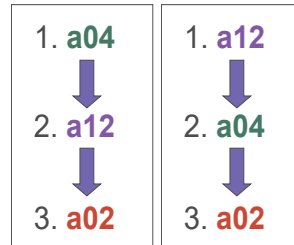
- Calculation components, e.g. aggregation operators, post-analysis elements, etc.
- Components with full MCDA methods
- Visualization components
- Reporting/comparison components

## What is nice about diviz (so far)?

- Access to **multiple methods**
- **Interface and logic is the same**, although methods may differ a lot
- **Construction** of MCDA workflows (=methods) from elementary components

### • Comparing logic and outcomes of different approaches

- compare rankings obtained with different methods by **visual means** or with **Kendall's coefficient**  
how many pairwise comparisons agreed/not?  
1 – full agreement, -1 – disagreement



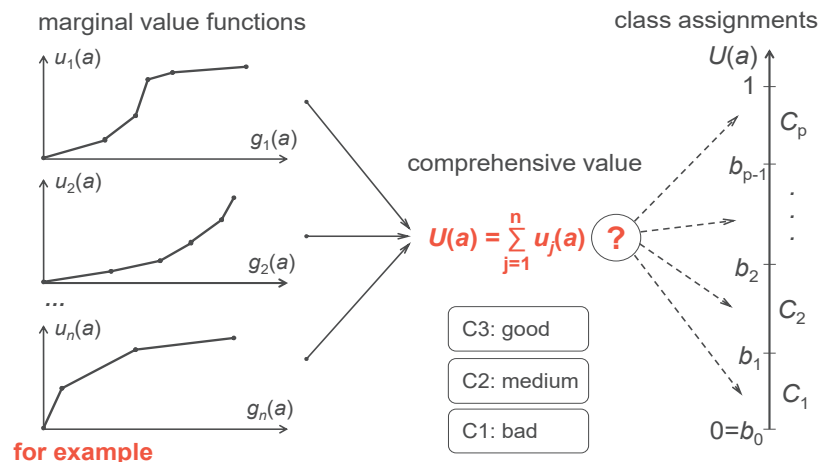
- **Easy to prepare input and share output**
  - workflow: import / export options

## diviz demo (3)



## TIME FOR DEMO COMPARING RESULTS OF DIFFERENT METHODS

## Threshold-based value driven sorting



## Basic Robust Ordinal Regression for sorting

### preference information

#### assignment examples

- *a12* should be assigned to class *good*:  $a12 \rightarrow C3$
- *a04* should not be assigned to class *bad*:  $a04 \rightarrow [C2, C3]$

### preference model

set of **all** value functions and class thresholds compatible with DM's preference

### results

#### assignments

- **necessary** assignment confirmed by all compatible models
- **possible** assignment confirmed by at least one compatible model

exploitation with linear programming



## Different types of input preference information

### assignment examples

a12 should be assigned to class *good*:  $a12 \rightarrow C3$

a04 should not be assigned to class *bad*:  $a04 \rightarrow [C2, C3]$

### assignment-based pairwise comparisons

a03 is better than a05 by at least one *class*

The class difference between a07 and a01 is at most one

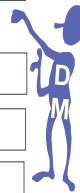
a11 and a12 should be assigned to the same *class*

### desired class cardinalities

At most 5 cars can be assigned to class *good*

At least 40% of cars should be assigned to class *bad*

The number of cars assigned to class *medium* should be between 3 and 7



## Different types of output sorting results

assignment examples  
assignment-based pair-wise comparisons  
desired class cardinalities

### preference information

set of **all** value functions and class thresholds  
compatible with DM's preference

exploitation with  
linear programming



### recommendation

**assignments**

**assignment-based  
preference relations**

**class  
cardinalities**

### variety of results

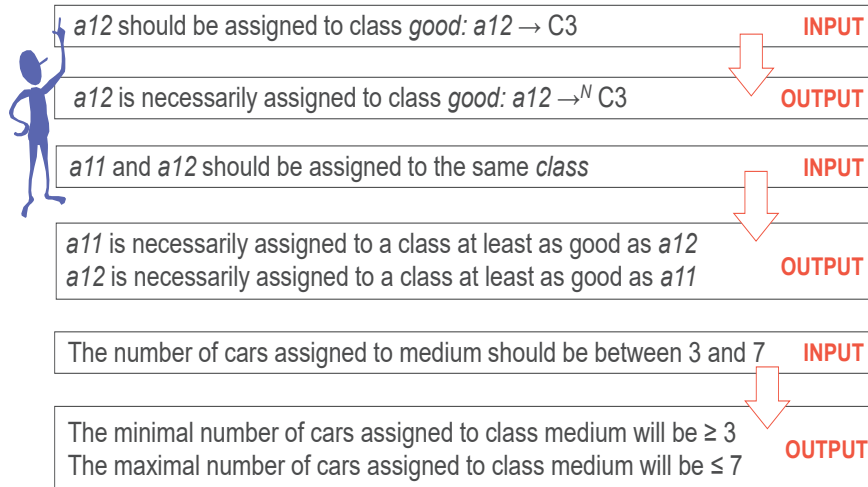
**necessary** = for all, **possible** = for at least one  
**extreme** = the most and the least advantageous

### for example:

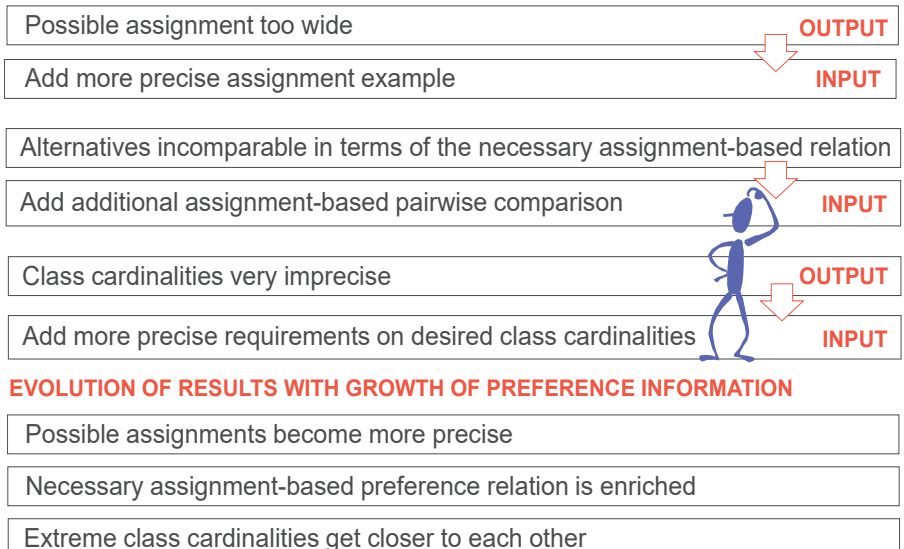
- necessary **assignment-based preference relation**:  
a05 is necessarily assigned to a class at least as good as a06
- extreme class cardinalities**:  
the **minimal/maximal number** of cars assigned to class medium is 5



## Preference information reflected in results



## Results motivate enrichment of preference information

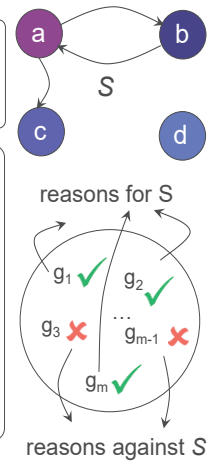




## TIME FOR DEMO ROR-UTADIS

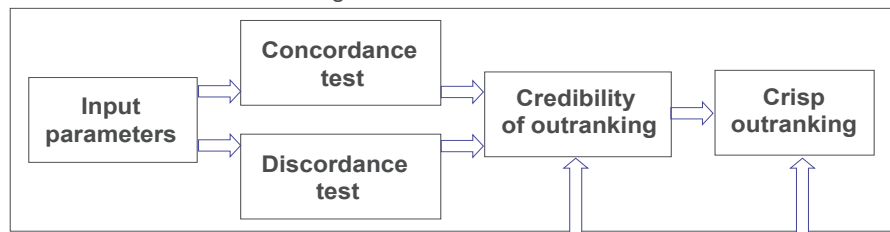
- **a outranks b** ( $aSb$ ) if the arguments of a decision maker in favour of the statement "a is at least as good as b" are strong enough and there arguments opposite to this statements are weak

- These arguments are based on:
  - The **evaluations** of a and b on the various criteria
  - **Information on the preference** of the decision maker: criteria weight ( $w_j$ ), indifference ( $q_j$ ), preference ( $p_j$ ), pre-veto (discordance) ( $pv_j$ ) and veto ( $v_j$ ) thresholds for each criterion, and cutting level ( $\lambda$ )
- **Remark:** if no argument can be found neither in favour of  $aSb$  nor in favour of  $bSa \rightarrow$  **incomparability**



## ELECTRE methods: step by step

### Construction of an outranking relation



### Exploitation of outranking relation in a way specific for ranking, choice or sorting

#### CHOICE

- ELECTRE I
- ELECTRE IV
- ELECTRE Is
- ...

#### RANKING

- ELECTRE II
- ELECTRE III
- ELECTRE IV
- ...

#### SORTING

- ELECTRE TRI-B
- ELECTRE TRI-C
- ELECTRE TRI-rC
- MR-SORT
- THESEUS

## Partial concordance indices

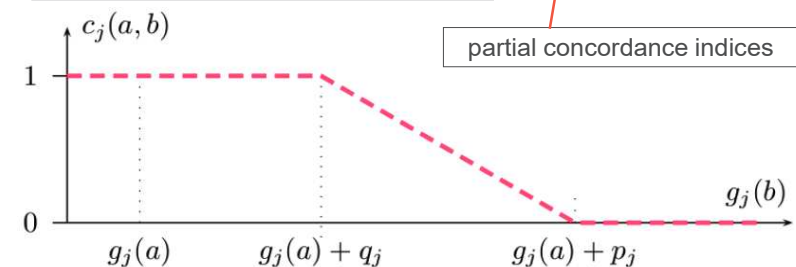
### Compute **partial concordance index** for each pair of alternatives

indifference threshold on criterion  $g_1$

for example, if  $g_1(a04) - g_1(a05) \geq -q_1 \Rightarrow c_1(a04, a05) = 1.0$

for example, if  $g_2(a05) - g_2(a04) \leq -p_2 \Rightarrow c_2(a04, a05) = 0.0$

preference threshold on criterion  $g_2$





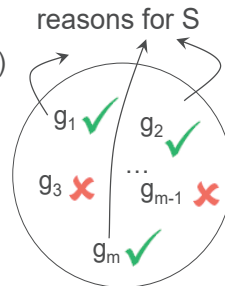
## Comprehensive concordance index

Compute **comprehensive concordance index** for each pair of objects:

the contribution of all criteria to the proposition  $aSb$

$$C(a,b) = \sum_j w_j \cdot c_j(a,b) = w_1 \cdot c_1(a,b) + w_2 \cdot c_2(a,b) + \dots + w_n \cdot c_n(a,b)$$

weight associated with criterion  $g_j$   
 $\sum_{j=1 \dots n} w_j = 1$



More advanced options account for:

- *Interactions* between criteria (mutual strengthening, mutual weakening, antagonistic effect)
- *Reinforced preference effect* (very strong reasons for  $S$ )

## Partial discordance indices

- **Compute partial discordance**: measures the degree to which a criterion is discordant (i.e., express opposition) with the proposition  $aSb$

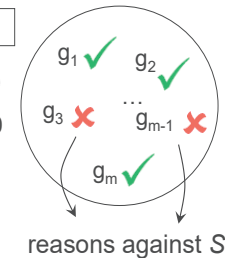
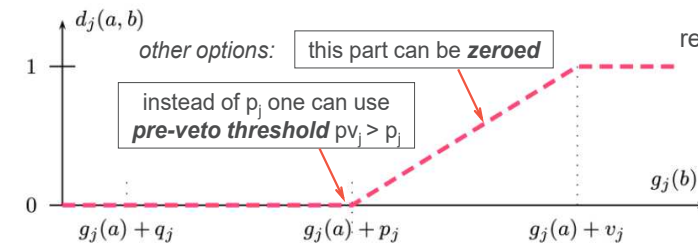
veto threshold on criterion  $g_1$

partial discordances

for example, if  $g_1(a05) - g_1(a04) \geq v_1 \Rightarrow d_1(a04, a05) = 1.0$

for example, if  $g_2(a05) - g_2(a04) \leq p_2 \Rightarrow d_2(a04, a05) = 0.0$

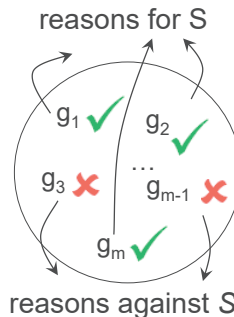
preference threshold on criterion  $g_2$



## Credibility = valued outranking relation

The (valued) outranking relation can be defined by a **credibility index**  $\sigma(a,b)$ :

- if no criterion is discordant:  $\sigma(a,b) = C(a,b)$
- if at least one criterion is discordant:  $\sigma(a,b) < C(a,b)$
- if  $d_j(a,b)=1$  for at least one criterion:  $\sigma(a,b) = 0$



**Formulation:**

$$\sigma(a,b) = C(a,b) \prod_{j \in F} \frac{1 - d_j(a,b)}{1 - C(a,b)}$$

where  $F = \{j : d_j(a,b) > C(a,b)\}$

also computable without weights as in ELECTRE IV

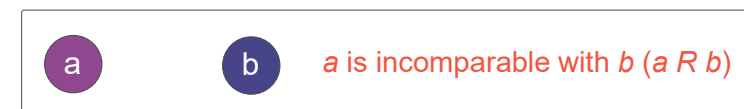
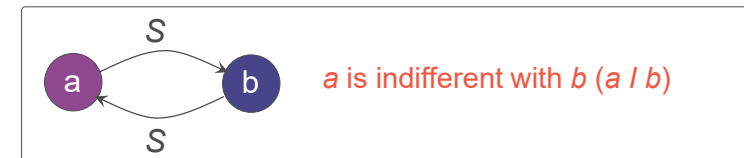
other options (no denominator):  
 instead of all sufficiently great arguments against outranking, account only for **the greatest (max) one** (not product, but max)

instead of all **sufficiently great** arguments against outranking, include **all** arguments against (no  $j \in F$ )

## Crisp outranking relation

Comparison of a credibility index with **cutting level  $\lambda$**  (is it high enough?)

$$\sigma(a,b) \geq \lambda \Rightarrow aSb$$



## Net Flow Score procedure

$$NFS(a) = \text{strength}(a) - \text{weakness}(a)$$

- exploitation of a **valued** outranking relation

$$NFS^\sigma(a) = \sum_{b \in A} [\sigma(a, b) - \sigma(b, a)]$$



$\sigma(a, b)$	a	b	c
a	-	0.8	0.4
b	0.6	-	0.7
c	0.3	0.4	-

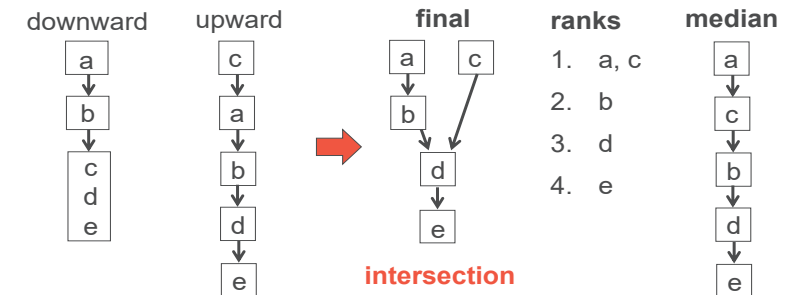
$$NFS^{Sval}(a) = 1.2 - 0.9 = 0.3$$

$$NFS^{Sval}(b) = 1.3 - 1.2 = 0.1$$

$$NFS^{Sval}(c) = 0.7 - 1.1 = -0.4$$

## ELECTRE III - distillation procedures

- distillation procedure** exploiting a valued outranking relation
- downward** pre-order (constructed top-down)
  - identify alternatives  $A_1$  with the greatest quality
  - put  $A_1$  at the top, and continue with  $A/A_1$ , etc.
- upward** pre-order (constructed bottom-up)
  - identify alternatives  $A_1$  with the least quality
  - put  $A_1$  at the bottom, and continue with  $A/A_1$ , etc.

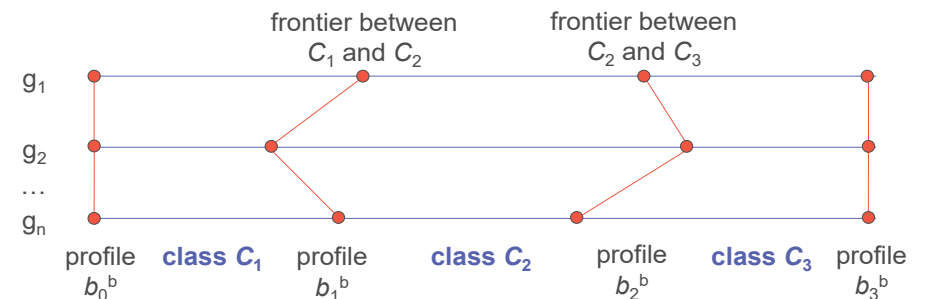


## diviz demo (5)

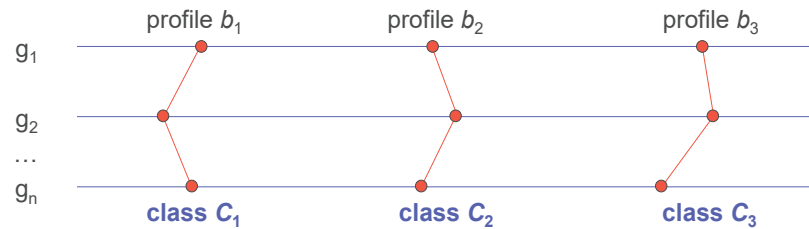


TIME FOR DEMO  
RANKING WITH ELECTRE

## ELECTRE TRI-B



- boundary profiles** used for modeling the frontiers between classes
- two **disjoint assignment rules** for assignment of alternative  $a$ 
  - pessimistic rule**
    - start from the **best** profile
    - find the first profile  $b_h^b : a \ S \ b_h^b$
    - select  $C_{h+1}$
  - optimistic rule**
    - start from the **worst** profile
    - find the first profile  $b_h^b : b_h^b > a$
    - select  $C_h$



- characteristic profiles formed from the class representative criteria values
- two conjoint assignment rules for assignment of alternative  $a$  indicating:
  - the worst class of  $a$ 
    - start from the second best profile
    - find the first profile  $b_h$ :  
 $a > b_h$  and  $\sigma(a, b_{h+1}) > \sigma(b_h, a)$
    - select  $C_{h+1}$
  - the best class of  $a$ 
    - start from the second worst profile
    - find the first profile  $b_h$ :  
 $b_h > a$  and  $\sigma(b_{h-1}, a) > \sigma(a, b_h)$
    - select  $C_{h-1}$
- indications of these two rules combined into a recommended class interval



## TIME FOR DEMO SORTING WITH ELECTRE

## What diviz is?

- tool for MCDA component workflow
- simple data visualization tool
- platform independent and open source



UTA, UTASTAR, ACUTA, UTAMP, Robust Ordinal Regression (UTA-GMS), RUTA, Extreme Ranking Analysis, SMAA-2, Stochastic Ordinal Regression  
**ROR-UTADIS** (including UTADIS-GMS)

**"Construct your own Electre"**  
**"Construct your own Promethee"**  
 over 1000 variants of Electre and Promethee

Aggregation operators: **weighted sum**, OWA, Choquet integral, etc.

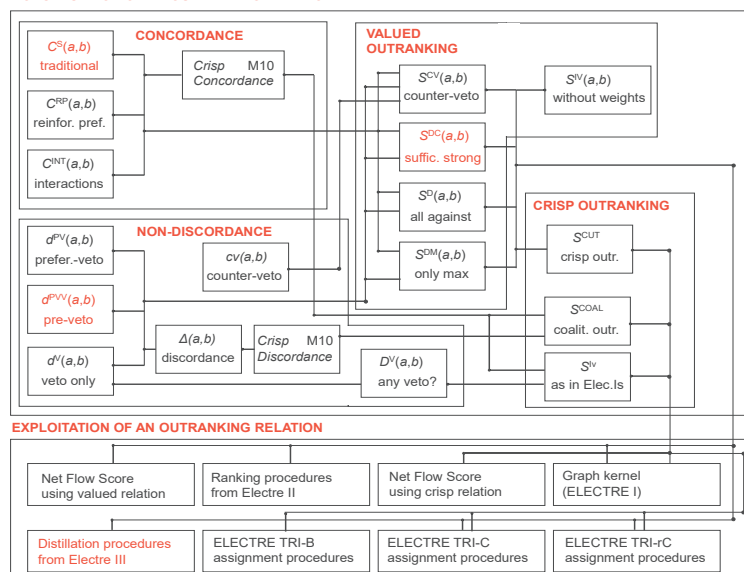
Rubis, MR-Sort, clustering

**Visualisation**, descriptive stats, reports, **comparison methods**, and many many more ☺

Data Envelopment Analysis: CCR and value-based model robust and stochastic analysis

## Construct your own ELECTRE

### CONSTRUCTION OF AN OUTRANKING RELATION



## Summary (1)

### Make MCDA software publicly available

- "I like the procedure described in this paper, where can I test it?"
- Both the traditional methods and brand new ones



### Decompose the MCDA methods into elementary components

- Give the possibility to create workflow of such components
- MCDA methods, algorithmic components and data visualization modules are available as web services
- Components can interoperate via the XMCD standard

### Have you ever wished what would happen if...?

### How do the results of one methods differ from these of another one?



### Expect more from us....

...on both visual and methodological sites



## Summary (2)

### How you can help the project?

- Join the Decision Deck Consortium
- Test the software & send us your opinion
- Let us know what you need



### Important websites

- <http://www.decision-deck.org>
  - <http://www.diviz.org>, @divizMCDA, +diviz - all information on diviz
  - getting help: <http://www.diviz.org/contact>
- S. Bigaret, P. Meyer, M. Kadziński, V. Mousseau, M. Pirlot, ...**



R. Bisdorff, L. Dias, P. Meyer, V. Mousseau, M. Pirlot, *Evaluation and Decision Models with Multiple Criteria*, Springer, 2015



## Hands on exercises

- **Construction** of some of the previously presented "method" in diviz
- Help Thierry to **choose the car** which is "best" for him
- 2 roles in each group:
  - The **analyst** constructs the MCDA algorithmic workflows
  - The **decision maker** (Thierry) is questioned by the analyst on his/her preferences

### Practical work (see detailed instructions)

- Multi-Attribute Value Theory (steps V)
- Electre III (steps E)
- Promethee (steps P)
- UTA (steps U)
- Comparing results (steps C)

