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International  
Handbooks  
on Information  
Systems

# HANDBOOK ON SCHEDULING

From Theory to Applications

 Springer

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# Handbook on Scheduling

From Theory to Applications

With 144 Figures and 28 Tables

 Springer

# Contents

<b>1</b>	<b>Introduction</b> .....	<b>1</b>
	References .....	7
<b>2</b>	<b>Basics</b> .....	<b>9</b>
2.1	Sets and Relations .....	9
2.2	Problems, Algorithms, Complexity .....	11
2.2.1	Problems and Their Encoding .....	11
2.2.2	Algorithms .....	13
2.2.3	Complexity .....	16
2.3	Graphs and Networks .....	21
2.3.1	Basic Notions .....	21
2.3.2	Special Classes of Digraphs .....	22
2.3.3	Networks .....	25
2.4	Enumerative Methods .....	32
2.4.1	Dynamic Programming .....	33
2.4.2	Branch and Bound .....	33
2.5	Heuristic and Approximation Algorithms .....	35
2.5.1	Approximation Algorithms .....	35
2.5.2	Local Search Heuristics .....	37
	References .....	52
<b>3</b>	<b>Definition, Analysis and Classification of Scheduling Problems</b> .....	<b>57</b>
3.1	Definition of Scheduling Problems .....	57
3.2	Analysis of Scheduling Problems and Algorithms .....	62
3.3	Motivations for Deterministic Scheduling Problems .....	65
3.4	Classification of Deterministic Scheduling Problems .....	68
	References .....	71
<b>4</b>	<b>Scheduling on One Processor</b> .....	<b>73</b>
4.1	Minimizing Schedule Length .....	73
4.1.1	Scheduling with Release Times and Deadlines .....	74
4.1.2	Scheduling with Release Times and Delivery Times .....	81
4.2	Minimizing Mean Weighted Flow Time .....	83
4.3	Minimizing Due Date Involving Criteria .....	95

4.3.1	Maximum Lateness .....	96
4.3.2	Number of Tardy Tasks .....	104
4.3.3	Mean Tardiness .....	109
4.3.4	Mean Earliness .....	113
4.4	Minimizing Change-Over Cost .....	114
4.4.1	Setup Scheduling .....	114
4.4.2	Lot Size Scheduling .....	117
4.5	Other Criteria .....	122
4.5.1	Maximum Cost .....	122
4.5.2	Total Cost .....	127
	References .....	130
<b>5</b>	<b>Scheduling on Parallel Processors .....</b>	<b>137</b>
5.1	Minimizing Schedule Length .....	137
5.1.1	Identical Processors .....	137
5.1.2	Uniform and Unrelated Processors .....	158
5.2	Minimizing Mean Flow Time .....	168
5.2.1	Identical Processors .....	168
5.2.2	Uniform and Unrelated Processors .....	169
5.3	Minimizing Due Date Involving Criteria .....	173
5.3.1	Identical Processors .....	173
5.3.2	Uniform and Unrelated Processors .....	179
5.4	Other Models .....	182
5.4.1	Scheduling Imprecise Computations .....	182
5.4.2	Lot Size Scheduling .....	185
	References .....	190
<b>6</b>	<b>Communication Delays and Multiprocessor Tasks .....</b>	<b>199</b>
6.1	Introductory Remarks .....	199
6.2	Scheduling Multiprocessor Tasks .....	205
6.2.1	Parallel Processors .....	205
6.2.2	Dedicated Processors .....	213
6.2.3	Refinement Scheduling .....	219
6.3	Scheduling Uniprocessor Tasks with Communication Delays .....	221
6.3.1	Scheduling without Task Duplication .....	222
6.3.2	Scheduling with Task Duplication .....	225
6.3.3	Scheduling in Processor Networks .....	226
6.4	Scheduling Divisible Tasks .....	228
	References .....	236

<b>7</b>	<b>Scheduling in Hard Real-Time Systems</b>	<b>243</b>
7.1	Introduction	243
7.1.1	What is a Real-Time System?	244
7.1.2	Examples of Real-Time Systems	245
7.1.3	Characteristics of Real-Time Systems	246
7.1.4	Functional Requirements for Real-Time Systems	247
7.2	Basic Notations	248
7.2.1	Structure of a Real-Time System	248
7.2.2	The Task Model	249
7.2.3	Schedules	250
7.3	Single Processor Scheduling	252
7.3.1	Static Priority Rules	253
7.3.2	Dynamic Priority Scheduling	262
7.4	Scheduling Periodic Tasks on Parallel Processors	264
7.5	Resources	265
7.6	Variations of the Periodic Task Model	266
	References	267
<b>8</b>	<b>Flow Shop Scheduling</b>	<b>271</b>
8.1	Introduction	271
8.1.1	The Flow Shop Scheduling Problem	271
8.1.2	Complexity	273
8.2	Exact Methods	274
8.2.1	The Algorithms of Johnson and Akers	274
8.2.2	Dominance and Branching Rules	277
8.2.3	Lower Bounds	278
8.3	Approximation Algorithms	282
8.3.1	Priority Rule and Local Search Based Heuristics	282
8.3.2	Worst-Case Analysis	285
8.3.3	No Wait in Process	289
8.4	Scheduling Flexible Flow Shops	291
8.4.1	Problem Formulation	291
8.4.2	Heuristics and Their Performance	294
8.4.3	A Model	296
8.4.4	The Makespan Minimization Problem	297
8.4.5	The Mean Flow Time Problem	311
	References	316

<b>9</b>	<b>Open Shop Scheduling</b> .....	<b>321</b>
9.1	Complexity Results .....	321
9.2	A Branch and Bound Algorithm for Open Shop Scheduling .....	323
9.2.1	The Disjunctive Model of the OSP .....	323
9.2.2	Constraint Propagation and the OSP .....	326
9.2.3	The Algorithm and Its Performance .....	332
	References .....	341
<b>10</b>	<b>Scheduling in Job Shops</b> .....	<b>345</b>
10.1	Introduction .....	345
10.1.1	The Problem .....	345
10.1.2	Modeling .....	345
10.1.3	Complexity .....	348
10.1.4	The History .....	349
10.2	Exact Methods .....	352
10.2.1	Branch and Bound .....	353
10.2.2	Lower Bounds .....	353
10.2.3	Branching .....	355
10.2.4	Valid Inequalities .....	358
10.3	Approximation Algorithms .....	360
10.3.1	Priority Rules .....	360
10.3.2	The Shifting Bottleneck Heuristic .....	362
10.3.3	Opportunistic Scheduling .....	365
10.3.4	Local Search .....	367
10.4	Conclusions .....	387
	References .....	388
<b>11</b>	<b>Scheduling with Limited Processor Availability</b> .....	<b>397</b>
11.1	Problem Definition .....	398
11.2	One Machine Problems .....	401
11.3	Parallel Machine Problems .....	403
11.3.1	Minimizing the Sum of Completion Times .....	403
11.3.2	Minimizing the Makespan .....	404
11.3.3	Dealing with Due Date Involving Criteria .....	412
11.4	Shop Problems .....	414
11.4.1	Flow Shop Problems .....	414
11.4.2	Open Shop Problems .....	417
11.5	Conclusions .....	417
	References .....	419

<b>12 Scheduling under Resource Constraints</b> .....	<b>425</b>
12.1 Classical Model .....	425
12.2 Scheduling Multiprocessor Tasks .....	436
12.3 Scheduling with Continuous Resources .....	450
12.3.1 Introductory Remarks .....	451
12.3.2 Processing Speed vs. Resource Amount Model .....	452
12.3.3 Processing Time vs. Resource Amount Model .....	461
12.3.4 Ready Time vs. Resource Amount Model .....	466
References .....	471
<b>13 Constraint Programming and Disjunctive Scheduling</b> .....	<b>477</b>
13.1 Introduction .....	477
13.2 Constraint Satisfaction .....	479
13.2.1 The Constraint Satisfaction and Optimization Problem .....	479
13.2.2 Constraint Propagation .....	481
13.3 The Disjunctive Scheduling Problem .....	493
13.3.1 The Disjunctive Model .....	494
13.3.2 Solution Methods for the DSP .....	497
13.4 Constraint Propagation and the DSP .....	497
13.4.1 Some Basic Definitions .....	498
13.4.2 Precedence Consistency Tests .....	500
13.4.3 Lower-Level Bound-Consistency .....	500
13.4.4 Input/Output Consistency Tests .....	509
13.4.5 Input/Output Negation Consistency Tests .....	516
13.4.6 Input-or-Output Consistency Tests .....	522
13.4.7 Energetic Reasoning .....	523
13.4.8 Shaving .....	527
13.4.9 A Comparison of Disjunctive Consistency Tests .....	528
13.4.10 Precedence vs. Disjunctive Consistency Tests .....	530
13.5 Conclusions .....	530
13.6 Appendix: Bound Consistency Revisited .....	531
References .....	535
<b>14 Scheduling in Flexible Manufacturing Systems</b> .....	<b>539</b>
14.1 Introductory Remarks .....	539
14.2 Scheduling Dynamic Job Shops .....	542
14.2.1 Introductory Remarks .....	542
14.2.2 Heuristic Algorithm for the Static Problem .....	543
14.2.3 Computational Experiments .....	549

14.3	Simultaneous Scheduling and Routing in some FMS .....	550
14.3.1	Problem Formulation .....	550
14.3.2	Vehicle Scheduling for a Fixed Production Schedule .....	552
14.3.3	Simultaneous Job and Vehicle Scheduling .....	557
14.4	Batch Scheduling in Flexible Flow Shops under Resource Constraints .....	559
14.4.1	Introduction - Statement of the Problem .....	559
14.4.2	Mathematical Formulation .....	560
14.4.3	Heuristic Solution Approach .....	570
14.4.4	Implementation and Computational Experiment .....	577
	References .....	579
<b>15</b>	<b>Computer Integrated Production Scheduling .....</b>	<b>583</b>
15.1	Scheduling in Computer Integrated Manufacturing .....	584
15.2	A Reference Model for Production Scheduling .....	589
15.3	IPS: An Intelligent Production Scheduling System .....	597
15.3.1	Interactive Scheduling .....	604
15.3.2	Knowledge-based Scheduling .....	619
15.3.3	Integrated Problem Solving .....	624
	References .....	628
	<b>Index .....</b>	<b>631</b>